

Nom :

## Feuille de formule – Électricité et magnétisme

### Constantes :

$$g = 9,8 \text{ m/s}^2 \quad e = 1,6 \times 10^{-19} \text{ C} \quad k = 9 \times 10^9 \text{ N} \cdot \text{m}^2 / \text{C}^2 \quad \epsilon_0 = 8,85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2) \quad \mu_0 = 4\pi \times 10^{-7} \text{ kg} \cdot \text{m/C}^2$$

$$c = 3 \times 10^8 \text{ m/s}$$

<u>Électron :</u>	<u>Proton :</u>	<u>Neutron :</u>	<u>Muon :</u>
$m_e = 9,11 \times 10^{-31} \text{ kg}$	$m_p = 1,67 \times 10^{-27} \text{ kg}$	$m_n = 1,67 \times 10^{-27} \text{ kg}$	$m_\mu = 1,88 \times 10^{-28} \text{ kg}$
$q_e = -e$	$q_p = +e$	$q_n = 0$	$q_\mu = -e$

### Formules :

$v_x(t) = \frac{dx(t)}{dt}$	$x(t) = x_0 + v_{x0}t + \frac{1}{2}a_x t^2$	$a_c = \frac{v^2}{r}$	$\omega_z(t) = \frac{d\theta_z(t)}{dt}$
$a_x(t) = \frac{dv_x(t)}{dt}$	$v_x(t) = v_{x0} + a_x t$	$v_x^2 = v_{x0}^2 + 2a_x(x - x_0)$	$\alpha_z(t) = \frac{d\omega_z(t)}{dt}$

$\sum \vec{F} = m\vec{a}$	$\vec{F}_g = m\vec{g}$	$g = G \frac{M}{r^2}$	$F_r = ke$	$f = \mu n$
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$\vec{F}_e = q\vec{E}$	$\vec{F}_e = k \frac{qQ}{r^2} \hat{r}$	$\vec{E} = k \frac{Q}{r^2} \hat{r}$	$\vec{E} = \int k \frac{dQ}{r^2} \hat{r}$
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$\vec{F}_m = q\vec{v} \times \vec{B}$	$\vec{F}_m = I \vec{\ell} \times \vec{B}$	$d\vec{F}_m = I d\vec{\ell} \times \vec{B}$	$\vec{B} = \int \frac{\mu_0}{4\pi} \frac{I d\vec{\ell} \times \hat{r}}{r^2}$
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$E = \frac{2k \lambda }{R}$	$E = \frac{ \sigma }{2\epsilon_0}$	$E = \frac{k Q }{D(D+L)}$	$E = \frac{2k \lambda }{R} \sin(\alpha)$	$E_\perp = \frac{k \lambda }{R}  \sin(\alpha_A) - \sin(\alpha_B) $	$E_\parallel = \frac{k \lambda }{R}  \cos(\alpha_A) - \cos(\alpha_B) $
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$B = \frac{\mu_0 I}{2\pi R}$	$B = \frac{\mu_0 I}{4\pi R}  \sin(\alpha_2) - \sin(\alpha_1) $	$B = N \frac{\mu_0 I}{2R}$	$B = N \frac{\mu_0 I}{2R} \sin^3(\alpha)$	$B = \frac{\mu_0 n I}{2}  \cos(\alpha_2) - \cos(\alpha_1) $
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$E_f = E_i + W_a$	$W = \int \vec{F} \cdot d\vec{s}$	$W = \vec{F} \cdot \vec{s}$	$E = K + U$	$K = \frac{1}{2}mv^2$
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$\vec{p}_f = \vec{p}_i + \vec{J}$	$\vec{J} = \int \vec{F} dt$	$\vec{J} = \vec{F} \Delta t$	$\vec{p} = m\vec{v}$	$\vec{F} = \frac{d\vec{p}}{dt}$
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$P = \frac{dE}{dt}$	$P = \vec{F} \cdot \vec{v}$	$E = \int P dt$	$U_r = \frac{1}{2}ke^2$	$U_g = mgy$	$U_g = -G \frac{mM}{r}$
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$W_c = -\Delta U$	$U_c = qV$	$U_c = k \frac{qQ}{r}$	$U_c = \sum_{i<j} k \frac{q_i q_j}{r_{ij}}$	$U_c = \frac{1}{2} \frac{kq^2}{r}$
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$\Delta V = -\int \vec{E} \cdot d\vec{s}$	$\Delta V = -\vec{E} \cdot \vec{s}$	$E_x = -\frac{dV}{dx}$	$V = k \frac{Q}{r}$	$V = V_{ref} - \vec{E} \cdot \vec{s}$	$V = -2k\lambda \ln\left(\frac{r}{[1m]}\right)$
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$C = \frac{q}{\Delta V}$	$U_c = \frac{1}{2}C\Delta V^2$	$C = KC_{vide}$	$E = \frac{E_{ext}}{K}$
$C_{vide} = \frac{\epsilon_0 A}{d}$	$C_{vide} = \frac{R}{k}$	$C_{vide} = \frac{R_A R_B}{k(R_A - R_B)}$	$C_{vide} = \frac{L}{2k \ln(R_B / R_A)}$

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$$\begin{array}{llllll} \Delta V = \frac{\Delta U_e}{q} & I = \frac{\Delta q}{\Delta t} & I = n A e v_d & \sum_i I_i = 0 & \sum_i \Delta V_i = 0 & Q = m C \Delta T \\ \Delta V = R I & R = \rho \frac{L}{A} & R_{\text{eq}} = \sum_i R_i & R_{\text{eq}} = \left[ \sum_i \frac{1}{R_i} \right]^{-1} & q = q_0 e^{-t/RC} & T_{1/2} = RC \ln 2 \\ P = I \Delta V & P = R I^2 & P = \frac{(\Delta V)^2}{R} & \bar{P} = \frac{1}{2} \frac{\varepsilon_0^2}{R} & \varepsilon_{\text{eff}} = \frac{\varepsilon_0}{\sqrt{2}} & \\ \\ \varepsilon_{\text{ind}} = v B \ell \sin \theta & \Phi_m = \vec{B} \cdot \vec{A} & \Phi_m = \int \vec{B} \cdot d\vec{A} & \varepsilon_{\text{ind}} = \left| \frac{d\Phi_m}{dt} \right| \end{array}$$

### Mathématique :

$$\begin{array}{ll} \vec{A} = (A_x, A_y, A_z) = A_x \vec{i} + A_y \vec{j} + A_z \vec{k} & \vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos(\theta) = A_x B_x + A_y B_y + A_z B_z \\ A = |\vec{A}| = \sqrt{A_x^2 + A_y^2 + A_z^2} & \vec{A} \times \vec{B} = |\vec{A}| |\vec{B}| \sin(\theta) \hat{n} = (A_y B_z - A_z B_y) \vec{i} - (A_x B_z - A_z B_x) \vec{j} + (A_x B_y - A_y B_x) \vec{k} \end{array}$$

$$ax^2 + bx + c = 0 \Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad C = 2\pi r, \quad A = \pi r^2, \quad A = 4\pi r^2, \quad V = 4\pi r^3 / 3$$

$$\sin^2(\theta) + \cos^2(\theta) = 1 \quad 2 \cos \theta \sin \theta = \sin(2\theta)$$

$$\ln(A) + \ln(B) = \ln(AB) \quad \ln(A) - \ln(B) = \ln\left(\frac{A}{B}\right)$$

### Table de dérivée et d'intégrale :

$$\frac{dx^n}{dx} = nx^{n-1} \quad \frac{de^{Ax}}{dx} = Ae^{Ax} \quad \frac{d \ln x}{dx} = \frac{1}{x} \quad \frac{d \cos x}{dx} = -\sin x \quad \frac{d \sin x}{dx} = \cos x \quad \frac{d \tan x}{dx} = \sec^2 x$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C \quad \int \frac{1}{x} dx = \ln|x| + C \quad \int e^{Ax} dx = \frac{e^{Ax}}{A} + C$$

$$\int \cos(x) dx = \sin(x) + C \quad \int \sin(x) dx = -\cos(x) + C \quad \int \tan(x) dx = \ln|\sec(x)| + C$$

$$\int \frac{1}{A^2 + x^2} dx = \frac{1}{A} \arctan\left(\frac{x}{A}\right) + C \quad \int \frac{x}{(A^2 + x^2)^{3/2}} dx = \frac{-1}{\sqrt{A^2 + x^2}} + C \quad \int \frac{1}{(A^2 + x^2)^{3/2}} dx = \frac{x}{A^2 \sqrt{A^2 + x^2}} + C$$

### Dérivée en chaîne :

$$\frac{d}{dx} f(y(x)) = \frac{df}{dy} \frac{dy}{dx}$$

### Dérivée d'un produit :

$$\frac{d}{dx} f(x) \cdot g(x) = \frac{df(x)}{dx} g(x) + f(x) \frac{dg(x)}{dx}$$

### Intégrale par parties :

$$\int u dv = uv - \int v du$$